NOTES 10.2 - ARCS, SEMICIRCLES, \& CENTRAL ANGLES
CENTRAL ANGLE:

THEOREM: SUM OF CENTRAL ANGLES
The sum of the measures of the central angles of a circle with no interior points in common is $360^{\circ}$.
EXAMPLE 1: Name the following.
The central angle:
The two arcs: $\qquad$


MINOR ARC:

MAJOR ARC:

Arcs are measured by their corresponding central angles.

## EXAMPLE 2:



- $m \angle \mathrm{PCM}=$ $\qquad$
- $m \mathrm{PM}=$ $\qquad$
- $m$ PNM $=$ $\qquad$
- What kind of arc is PM? How do you know? $\qquad$
SEMICIRCLES:

EXAMPLE 3: In circle $\mathrm{E}, \mathrm{m} \angle \mathrm{AEN}=18^{\circ}, \overline{\mathrm{JN}}$ is a diameter, and $m \angle \mathrm{JES}=\mathbf{9 0}^{\circ}$. Find each measure.
a) $m \overparen{\mathrm{AN}}=$ $\qquad$
b) $m \widehat{\mathrm{JA}}=$ $\qquad$
c) $m \overparen{\mathrm{JAS}}=$ $\qquad$


EXAMPLE 4: $\overrightarrow{\mathrm{FD}}$ is a tangent to circle $\mathbf{0}$. Based on the angle measures
given, find the measure of each of the following.
a) $m \overparen{\mathrm{AB}}=$
b) $m \overparen{\mathrm{AD}}=$
$\qquad$
c) $m \overparen{\mathrm{AC}}=$
$\qquad$
d) $m \overparen{\mathrm{BC}}=$ $\qquad$
e) $m \overparen{\mathrm{ADC}}=$ $\qquad$
f) $m \overparen{A C D}=$ $\qquad$
g) $m \overparen{\mathrm{ED}}=$ $\qquad$
h) $m \overparen{\mathrm{AE}}=$ $\qquad$

i) $m \angle \mathrm{DOF}=$ $\qquad$
j) $m \angle E O A=$ $\qquad$
EXAMPLE 5: Find the measure of each of the following.
a) $m \angle A O B=$ $\qquad$
b) $m \angle \mathrm{BOC}=$ $\qquad$
c) $m \angle \mathrm{COD}=$ $\qquad$
d) $m \angle \mathrm{AOD}=$ $\qquad$


Notes 10.2 - Arcs, Semicircles, \& Central Angles (Continued)
EXAMPLE 6: Find the measure of each arc in circle C and classify it. In the figure $\overline{\mathrm{PZ}}$ is a diameter.
a) $m \overparen{P N}=$ $\qquad$ ;
b) $m \overparen{\mathrm{ZQP}}=$ $\qquad$ ; $\qquad$
c) $m \overparen{R Z}=$ $\qquad$ ; $\qquad$
d) $m \overparen{\mathrm{ZMP}}=$ $\qquad$ ;
e) $m \mathrm{RM}=$ $\qquad$ ; $\qquad$

f) $m \overparen{\mathrm{NQP}}=$ $\qquad$ ;
g) $m \overparen{Q N}=$ $\qquad$ ;
h) $m \overparen{R P}=$ $\qquad$ ; $\qquad$

EXAMPLE 7: Find the indicated measures.
$\boldsymbol{x}=$ $\qquad$
$m \angle A E B=$ $\qquad$
$m \angle B E C=$ $\qquad$
$m \angle C E D=$ $\qquad$
$m \angle$ DEA $=$ $\qquad$


