

17.2 – Multiplying & Dividing Functions

Function Operations	
Multiplication	$(f \cdot g)(x) = f(x) \cdot g(x)$
Division	$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}, g(x) \neq 0$

Examples:

1. Let $f(x) = x^2$ and $g(x) = x + 1$.

$$(f \cdot g)(x) = \underline{x^3 + x^2}$$
$$f(x) \cdot g(x) = x^2(x+1) = x^3 + x^2$$

$$\left(\frac{f}{g}\right)(x) = \underline{\frac{x^2}{x+1}}, \quad x \neq -1$$

$$\frac{f(x)}{g(x)} = \frac{x^2}{x+1} \quad \begin{aligned} g(x) &\text{ cannot equal } 0! \\ \text{If } x+1 &= 0, \\ \text{then } x &= -1. \text{ So, } x \text{ cannot be } -1! \end{aligned}$$

2. Let $f(x) = 7x - 5$ and $g(x) = 2x$.

$$(f \cdot g)(x) = \underline{14x^2 - 10x}$$
$$f(x) \cdot g(x) = (7x-5)(2x) = 14x^2 - 10x$$

$$\left(\frac{f}{g}\right)(x) = \underline{\frac{7x-5}{2x}}, \quad x \neq 0$$

$$\frac{f(x)}{g(x)} = \frac{7x-5}{2x} \quad \begin{aligned} g(x) &\text{ cannot equal } 0! \\ \text{If } 2x &= 0, \\ \text{then } x &= 0. \\ \text{So, } x &\text{ cannot be } 0! \end{aligned}$$