

## NOTES 7.5: TRAPEZOIDS & KITES

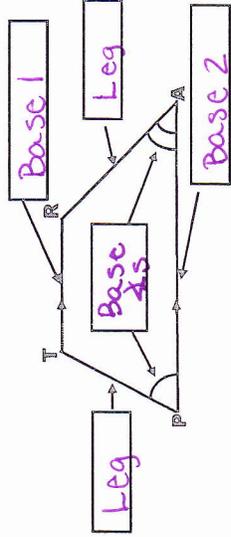
Objective: I can use properties of trapezoids & kites to find side lengths & measures.

### TRAPEZOID:

A quadrilateral with one pair of parallel sides

**BASES:** The parallel sides  
**LEGS:** The non-parallel sides

**BASE ANGLES:** The  $\angle$ s at the bases



- $\angle$  T &  $\angle$  P are supplementary
- $\angle$  R &  $\angle$  A are supplementary

**ISOSCELES TRAPEZOID:** A trapezoid in which the legs are  $\cong$ .



\* The base angles of an isosceles trapezoid are congruent.

The diagonals of an isosceles trapezoid also have a special relationship...

Graph the isosceles trapezoid MATH by plotting the points:

M(0, -2); A(0, 5); T(6, 7); H(6, -4).

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Name the diagonals of trapezoid MATH:

MT & AH

Find the length of each diagonal:

$$MT = \sqrt{(6-0)^2 + (7+2)^2}$$

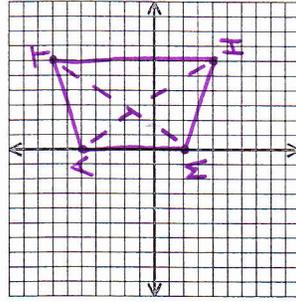
$$= \sqrt{36+81}$$

$$= \sqrt{117}$$

$$AH = \sqrt{(0-6)^2 + (5+4)^2}$$

$$= \sqrt{36+81}$$

$$= \sqrt{117}$$

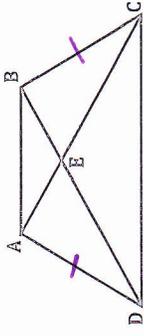


What can you say about the length of each diagonal? They are  $\cong$ .

What conclusion can you make? The diagonals of an isosceles trapezoid are  $\cong$ .

### EXAMPLE 1:

ABCD is an isosceles trapezoid. Decide whether each statement is TRUE or FALSE and explain.



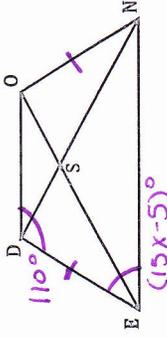
a)  $AC = BD$  True-Diagonals  $\cong$

b)  $\overline{AD} \cong \overline{BC}$  True-Legs  $\cong$

c)  $\overline{CA}$  and  $\overline{BD}$  bisect each other False- Not a parallelogram

### EXAMPLE 2:

DONE is an isosceles trapezoid.  $m\angle EDO = 110^\circ$  and  $m\angle DEN = (15x - 5)^\circ$ . Find the value of 'x':



Con These  $\angle$ s are supplementary!

$$110 + 15x - 5 = 180$$

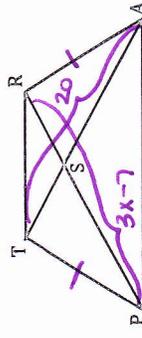
$$15x + 105 = 180$$

$$15x = 75$$

$$x = 5$$

### EXAMPLE 3:

TRAP is an isosceles trapezoid.  $PR = 3x - 7$  and  $TA = 20$ . Find the value of 'x'.



Diagonals are  $\cong$ !

$$3x - 7 = 20$$

$$3x = 27$$

$$x = 9$$

Notes 7.5 (Continued)

**MEDIAN:** The segment that joins the midpoints of the legs

MEDIAN =  $\frac{\text{Base 1} + \text{Base 2}}{2}$

**EXAMPLE 4:**

In trapezoid ABCD, EF is a median. Find each of the following.

a)  $AB = 25$ ,  $DC = 13$ ,  $EF = 19$   
 $\frac{13+25}{2} = \frac{38}{2} = 19$

b)  $AE = 11$ ,  $FB = 8$ ,  $AD = 22$ ,  $BC = 16$

c)  $AB = 29$ ,  $EF = 24$ ,  $DC = 19$   
 $24 = \frac{DC+29}{2}$   $48 = DC+29$   $19 = DC$

d)  $AB = 7y+6$ ,  $EF = 5y-3$ ,  $DC = y-2$ ,  $y = 5$   
 $5y-3 = \frac{7y+6+y-2}{2}$   $2(5y-3) = 7y+6+y-2$   
 $10y-6 = 8y+4$   $2y = 10$   
 $y = 5$

**EXAMPLE 5:**

Find the value of 'x' for the trapezoid.

$x = \frac{24+34}{2} = \frac{58}{2} = 29$

**EXAMPLE 6:**

Find the value of 'x' for the trapezoid.

$2x+3 = \frac{12+30}{2}$   $2x = 18$   
 $2x+3 = 21$   $x = 9$

To summarize, what can we say about all trapezoids?

- 1) One pair of parallel sides
  - 2) Median =  $\frac{\text{Base 1} + \text{Base 2}}{2}$
- In addition to these, what can we say about isosceles trapezoids?
- 1) Legs are  $\cong$
  - 2) Diagonals are  $\cong$
  - 3) Base  $\angle$ s are  $\cong$  (2 pairs)

**KITE:** A quadrilateral that has 2 pairs of consecutive  $\cong$  sides

- \* Exactly one pair of opposite  $\angle$ s is  $\cong$ . ( $\angle HGF \cong \angle HJF$ )
- \* Diagonals are  $\perp$ . ( $\overline{GJ} \perp \overline{HF}$ )
- \* Long diagonal bisects short diagonal & opposite  $\angle$ s. ( $\overline{GA} \cong \overline{AJ}$  &  $\angle GFH \cong \angle JFH$ )

**Example 1:**

In kite ABCD,  $m\angle BCD = 98^\circ$  and  $m\angle ADE = 47^\circ$ . Find each measure.

$m\angle DAE = 43^\circ$  (Diagonals are  $\perp$ .  $m\angle DAE = 90 - 47$ )  
 $m\angle BCE = 55^\circ$  ( $m\angle DAE = m\angle DCE$ )  
 $m\angle ABC = 70^\circ$  ( $m\angle BCD - m\angle DCE = m\angle BCE$ )  
 $m\angle BCE = m\angle BAE$  ( $98 - 43 = m\angle BCE$ )  
 $180 = m\angle BCE + m\angle BAE + m\angle ABC$   
 $180 = 55 + 55 + m\angle ABC$