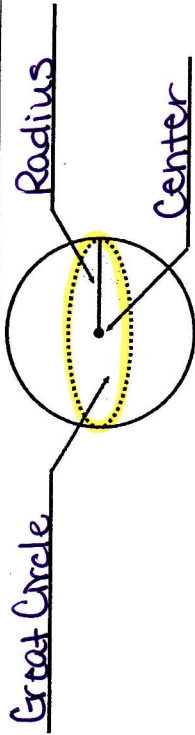


NOTES 12.6
SURFACE AREA & VOLUME OF SPHERES



FORMULAS

SURFACE AREA:

$$SA = 4\pi r^2$$

VOLUME:

$$V = \frac{4}{3}\pi r^3$$

EXAMPLE 1: Find the EXACT Surface Area of a sphere with a radius of 4 cm.

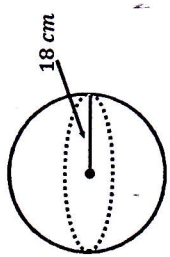
$$SA = 4\pi r^2$$

$$= 4\pi(4)^2$$

$$= 64\pi$$

$$SA = \underline{64\pi \text{ cm}^2}$$

EXAMPLE 2: Find the EXACT Volume of the sphere below.



$$V = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi(18)^3$$

$$= 7776\pi$$

$$V = \underline{7776\pi \text{ cm}^3}$$

EXAMPLE 3: A sphere has a diameter of 12 cm. Find its Surface Area and Volume.

$$SA = 4\pi r^2$$

$$= 4\pi(6)^2$$

$$SA = \underline{144\pi \text{ cm}^2}$$

$$V = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi(6)^3$$

$$V = \underline{288\pi \text{ cm}^3}$$

EXAMPLE 4: If a sphere has a volume of $\frac{4000\pi}{3}$ cubic units. Find its radius, diameter, and Surface Area.

$$V = \frac{4}{3}\pi r^3$$

$$\frac{4000\pi}{3} = \frac{4}{3}\pi r^3$$

$$1000\pi = 4\pi r^3$$

$$1000 = r^3$$

$$10 = r$$

$$r = \underline{10}$$

$$d = \underline{20}$$

$$SA = \underline{400\pi}$$

$$SA = 4\pi r^2$$

$$= 4\pi(10)^2$$

$$= 400\pi$$

EXAMPLE 5: If a sphere has a Surface Area of 64π square units, find its radius, diameter, and Volume.

$$SA = 4\pi r^2$$

$$64\pi = 4\pi r^2$$

$$16 = r^2$$

$$4 = r$$

$$r = \underline{4}$$

$$d = \underline{8}$$

$$V = \underline{\frac{256}{3}\pi}$$

$$V = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi(4)^3$$

$$= \frac{4}{3}\pi(64)$$

$$= \frac{256}{3}\pi$$

EXAMPLE 6: If the great circle of a sphere has a circumference of 32π units. Find the Surface Area and Volume of the sphere.

$$SA = 4\pi r^2$$

$$= 4\pi(16)^2$$

$$SA = \underline{1024\pi}$$

$$V = \underline{\frac{16384}{3}\pi}$$

$$C = 2\pi r$$

$$32\pi = 2\pi r$$

$$16 = r$$

$$V = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi(16)^3$$

$$= \frac{16384}{3}\pi$$