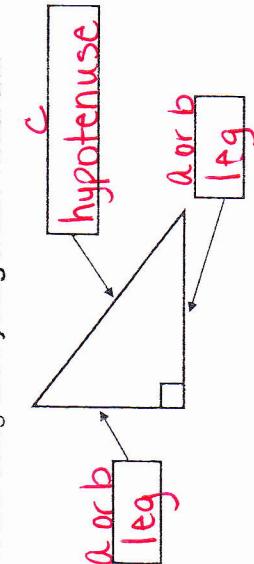


## NOTES 9.1: PYTHAGOREAN THEOREM

When two of three sides of a right triangle are known, the third side can be found using the *Pythagorean Theorem*.



$$\begin{aligned} a^2 + b^2 &= c^2 \\ \text{leg}^2 + \text{leg}^2 &= \text{hyp}^2 \end{aligned}$$

EXAMPLE 1: Find the value of ' $x$ '.

$$\begin{aligned} 3^2 + 7^2 &= x^2 \\ 9 + 49 &= x^2 \\ 58 &= x^2 \\ \sqrt{58} &= x \end{aligned}$$

1 leg  
hyp

EXAMPLE 4: Is 3, 4, 5 a Pythagorean Triple?

Any group of three positive integers  $a$ ,  $b$ , and  $c$ , such that  $c^2 = a^2 + b^2$  is known as a *Pythagorean Triple*.

EXAMPLE 5: Determine if a triangle can be formed when:

Classify:		Classify:	
(a) 5, 12, 4	YES or NO	(b) 6, 7, 8	YES or NO
(c) 1, 3, $\sqrt{10}$	YES or NO	(d) $\sqrt{9}, \sqrt{16}, \sqrt{27}$	YES or NO

Recall that one way to classify triangles is by *angles*. A triangle can be *acute*, *obtuse*, or *right*.

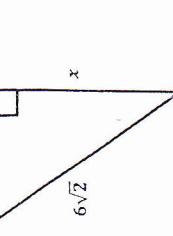
If a triangle can be formed, you can determine the type of triangle formed by comparing the square of the longest side ( $c$ ) to the sum of the squares of the shorter sides ( $a$  &  $b$ ).

$$\begin{aligned} \text{A } \text{RIGHT TRIANGLE} &\text{ can be formed when: } a^2 + b^2 = c^2 \\ \text{An } \text{ACUTE TRIANGLE} &\text{ can be formed when: } a^2 + b^2 > c^2 \\ \text{An } \text{OBTUSE TRIANGLE} &\text{ can be formed when: } a^2 + b^2 < c^2 \end{aligned}$$

EXAMPLE 5: Determine if a triangle can be formed, and if so, classify it.

(a) 5, 12, 4		(b) 6, 7, 8	
YES or NO		YES or NO	

EXAMPLE 3: Find the value of ' $x$ '.



(c) 1, 3, $\sqrt{10}$		(d) $\sqrt{9}, \sqrt{16}, \sqrt{27}$	
YES or NO		YES or NO	

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